# NASA TECHNICAL MEMORANDUM



# THERMODYNAMIC AND SHOCK PROPERTIES OF A SIMULATED JOVIAN ENTRY ATMOSPHERE

by Sheldon Heimel Lewis Research Center Cleveland, Ohio August, 1971

This information is being published in preliminary form in order to expedite its early release.

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# THERMODYNAMIC AND SHOCK PROPERTIES OF A SIMULATED JOVIAN ENTRY ATMOSPHERE

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# SUMMARY

The thermodynamic properties of the equilibrium plasma behind normal shock waves (incident and reflected) in a 0.70 Ne-.25H<sub>2</sub>-.05He mixture were computed for assigned shock velocities from 5 to 15 km/sec and pressures from 0.05 to 1.0 mm Hg. Equilibrium pressure, temperature, enthalpy, entropy, constant-pressure heat capacity, and component mole fractions are tabulated for an initial temperature of 298.15K. The free energy of the mixture was minimized to obtain composition. The Debye-Huckel approximation was used to account for ionization-potential lowering and partition-function cutoff.

#### INTRODUCTION

Basic data concerning the atmosphere of Jupiter is needed to provide a better understanding of the evolution of our solar system. Because of its low atmospheric temperature (around 100 K) and its great size, it is thought that Jupiter has kept its primordial condition to a great extent.

To obtain these data, the National Academy of Science has highly recommended a Jovian atmospheric probe. Scientific experiments have been proposed for such a probe during the 1977 Grand Tour of the outer planets (ref. 1).

Entry of a probe into the hydrogen-helium Jovian atmosphere would cause shock-ionization of that mixture because of the probe's high entry speed.

Actual entry conditions are expected to involve shock velocities as high as 60 km/sec and temperatures as high as 50 000 K.

Survival of the probe requires proper design of a heat shield. This can be facilitated by simulating the expected conditions in the laboratory and subjecting test probes to these conditions. While these conditions cannot be approached in a conventional shock tube using a H2-He mixture, they can be simulated by raising the mixture's molecular weight and using a reflected shock wave. The molecular weight is raised by "bathing" the H2-He mixture in neon, for example, which does not react with hydrogen or helium.

Accordingly, calculations were performed for the thermodynamic properties following passage of incident and reflected shocks through a 0.70 Ne-0.25 H<sub>2</sub>-0.05 He atmosphere. The calculation included the Coulombic contribution to the equilibrium thermodynamic properties and the extrapolation of atomic energy levels up to the lowered ionization potential. These properties are used together with the appropriate conservation equations to obtain properties behind the incident and reflected shock waves.

The properties assigned to the cold gas ahead of the shock (condition 1) are:  $T_1 = 298.15 \text{ K}$ ,  $P_1 = 1.0$ , 0.8, 0.4, 0.2, 0.1, and 0.05 mm Hg and  $u_1 = 15$ , 12, 10, 8, 6.5, and 5 km/sec. (Symbols are defined in the symbol list.) These properties permit calculation of initial values of Mach number, H/RT, S/R, M,  $C_p/R$ ,  $X_s$ , and sonic velocity.

Conditions behind the incident and reflected shock fronts are designated condition 2 and condition 5 respectively.

The properties from the incident shock calculation are:  $u_2$ ,  $P/P_0$ , T, H/RT, S/R, M,  $(\partial \ln V/\partial \ln P)_T$ ,  $(\partial \ln V/\partial \ln T)_p$ ,  $C_p/R$ ,  $X_s$ ,  $X_s$ , sonic velocity; the Coulombic parameters: ionization potential lowering, Debye length, DEBN/BETN (ratio of principal quantum numbers for Debye and Bethe cutoffs); number of charged particles in the Debye sphere, Coulombic compressibility; ratios across the incident shock:  $P_2/P_1$ ,  $T_2/T_1$ ,  $M_2/M_1$ ,  $P_2/P_3$ ;  $v_2 = u_1 - u_2$ , mole fractions and total particle density; the negative excess thermodynamic properties:  $-(H/RT)_{Coulombic}$  and  $-(S/R)_{Coulombic}$ 

Similar properties are calculated for the reflected shock wave. In this case the ratios are from condition 5 to condition 2 and, instead of  $v_2$ , the velocity  $u_5 + v_2$  is given.

# SYMBOLS

BETN	principal quantum number at Bethe cutoff
C	velocity of light
c <sub>p</sub>	heat capacity of mixture at constant pressure
C <sub>V</sub> .	heat capacity of mixture at constant volume
DEBN	principal quantum number at Debye-Huckel cutoff
е	electronic charge
G	Gibbs free energy of mixture
Н	enthalpy of mixture
h	Planck's constant
1	ionization potential
k	Boltzmann's constant
M	molecular weight of mixture
Ni	number of particles of species i
n	total number of moles in mixture
ni	number of moles of species i
P	absolute pressure
R	universal gas constant
S	entropy of mixture
T	absolute temperature
u	velocity in shock-fixed coordinates
V	volume
٧	velocity in laboratory coordinates
$W_{R}$	reflected shock velocity
W <sub>.</sub> 's	incident shock velocity

```
Z
          Coulomb compressibility
          signed charge number of species i
Ζį
                                  Greek Symbols
8
          Cp/Cv
          isentropic exponent; \chi_S = -(\partial \ln P/\partial \ln V)_S
 8<sub>S</sub>
 Δ
          lowering, as applied to ionization potential
          reciprocal of Debye length; \mathcal{K} = 1/\rho_{D}
 K
  P
          density of mixture
  PD
          Debye length
                                     Indices
          dummy index for species
i,j
                                   Subscripts
0
          property at one atmosphere
          ahead of incident shock
1
2
          behind incident shock
5
          behind reflected shock
R
          reflected shock
S
          isentropic; incident shock
```

# EQUATIONS DESCRIBING CHEMICAL EQUILIBRIUM

Values of the fundamental constants were obtained from reference 2.

The equilibrium composition of the plasma at an assigned T and P was calculated by minimizing the Gibbs free energy G of a closed, neutral system subject to the conservation of elements and charge. Minimization of G resulted in a system of equations that are non-linear in the number of moles of the constituents. Lagrangian multipliers were used to include the mass balance constraints. Application of the Newton-Raphson method resulted in a set of iteration equations in terms of the Lagrangian multipliers and corrections to the mole numbers. These working equations were taken from reference 3 and programmed for use with a high-speed computer.

The Debye-Hückel corrections (see below) to the Helmholtz free energy, pressure, and thermodynamic functions (H, S and G) and the thermodynamic derivatives (( $\frac{3 \ln V}{3 \ln T}$ )<sub>P</sub>, ( $\frac{3 \ln V}{3 \ln P}$ )<sub>T</sub>, ( $\frac{3 \ln v_i}{3 \ln P}$ )<sub>T</sub>, etc) were taken from reference 4.

# Assumptions and Restrictions

1. The species assumed to be present in the simulated Jovian entry atmosphere were: for hydrogen, H, H<sup>+</sup>, H<sub>2</sub>, H<sub>2</sub><sup>+</sup>, H<sup>-</sup>; for helium, He, He<sup>+</sup>, He<sup>++</sup>; for neon, Ne, Ne<sup>+</sup>, Ne<sup>+++</sup>, Ne<sup>+++</sup>; and electrons, e<sup>-</sup>. Only the ground state was used for H<sub>2</sub>; at those conditions where excited H<sub>2</sub> was beginning to comprise a significant proportion of total H<sub>2</sub>, total H<sub>2</sub> was unimportant. Excited electronic states of H<sub>2</sub><sup>+</sup> were neglected. The species H<sub>3</sub><sup>+</sup> was not included because its molecular constants are rough estimates (ref. 5) and yield unrealistic heat capacities.

2. Electronically excited states of H, He, He<sup>+</sup>, Ne, Ne<sup>+</sup>, and Ne<sup>++</sup> were included. In order to avoid divergence of the partition function, the cutoff of electronic levels was calculated by Griem's extension of the Debye-Huckel electrolytic theory (ref. 6). For small amounts of ionization, the size of the electron's orbit becomes unrealistically large. Therefore, in this instance the Debye-Huckel theory provides a poor criterion for cutoff. For this situation, Bethe's excluded volume criterion was used (ref. 7). In practice, the principal quantum number at each cutoff was calculated: BETN at the Bethe cutoff, and DEBN at the Debye-Huckel cutoff. The ratio DEBN/BETN was used to choose the method that truncated most states. If the ratio exceeded 1, then the Bethe cutoff was used. Otherwise the Debye-Huckel cutoff was used.

The Debye-Hückel method makes no cutoff provision for uninegative ions; thus a fixed number of excited states was used for H.

- 3. The Debye-Hückel theory was also used to account for Coulombic interactions between charged particles (ref. 4). These interactions yield real-gas corrections to the chemical potentials and the equation of state. When the Coulombic interactions became negligible, the plasma was treated as an ideal gas.
- 4. Shifts of energy levels of excited states relative to ground electronic states were neglected. These shifts are observed to be small (ref. 8).
- 5. Atomic sublevels for observed principal quantum numbers were interpolated by the "inclusion of predicted levels" technique (ref. 9) and extrapolated by the Rydberg formula (ref. 6) up to the reduced ionization potential.

# Electronic Partition Function and Ionization Potential

In the ideal-gas or independent-particle approximation, a bound electron moves under the influence of a single atomic species and has access to an infinite number of energy levels that approach the series limit. If all these levels were used in calculating the electronic partition function, it would diverge.

In a plasma, there is a Coulombic field due to the presence of ions and electrons. This field limits the set of energy levels available to the bound electron. Consequently the partition function terminates at the last level allowed. Also, the ionization potential is lowered and the amount of ionization is increased.

There is no exact procedure for specifying the last level to be permitted. In the present work, the Debye-Huckel approximation is used because it also affords a Coulombic correction to the Helmholtz free energy. This yields a consistent set of corrections to the chemical potentials, thermodynamic functions, and the equation of state.

In the Debye-Huckel cutoff (ref. 6), a level is not counted in the partition function if its energy exceeds the lowered ionization potential given by  $I - \Delta I$  where I is the unperturbed ionization potential of the species considered, and  $\Delta I$  is the lowering defined by

$$\Delta I = (z_i + 1) \int ke^2/hc$$
 (cm<sup>-1</sup>)

# Inclusion of Predicted Levels

Under certain conditions, theoretically predicted energy levels which have not been observed for atomic species must be included in the calculation of partition functions. The procedure used to estimate the significant levels depends somewhat on the temperature of the gas mixture.

At temperatures below about 5000 to 6000 K, it generally suffices to note the observed levels for a given principal quantum number and then to interpolate the missing levels. For this purpose, the "fill" method detailed in reference 9 was used.

At the higher temperatures typical of plasmas, quantum numbers for which no levels have been observed are occasionally required. At these higher quantum numbers, the Rydberg formula for hydrogenic levels (ref. 6) is a good approximation:

$$E_{n,y} = I_y - \frac{(z_i + 1)^2}{n^2} I_H$$

where  $E_{n,y}$  is the extrapolated energy level of atomic species y for principal quantum number n;  $I_y$  is its classical ionization potential;  $z_i$  is its charge number.  $I_H$  is the ionization potential of the H atom. The Rydberg formula was used for He and the neon species.

For the isoelectronic species H and He<sup>+</sup> the Bohr formula (ref. 10) was used:

$$E_{n,y} = I_v (1 - 1/n^2)$$

As explained below, interpolated levels were used in the first stage of the calculation; in the second stage, the levels were also extrapolated up to the reduced ionization potential.

# Accuracy of Composition

The Debye-Huckel approximation can be expected to be valid down to particle densities fulfilling the inequality

$$\frac{1}{5} \frac{\Lambda}{N!} > \frac{1}{100} 3$$

where  $\rho_{\rm D}$  is the Debye length and the summation is over charged particles (ref. 6). If V is taken to be the volume of the Debye sphere, i.e.

$$V = (4/3)\pi \rho_{\rm p}^{3}$$

then the total number of charged particles in the Debye sphere must obey the inequality

As  $\underset{L}{\xi}_{N_i}$  approaches 1/6, the accuracy can be expected to decrease. For the conditions of this report,  $\underset{L}{\xi}_{N_i}$  was never less than 2.67.

# Criterion for Using Ideal-Gas Approximation

At temperatures below approximately 4000 K, the degree of ionization was so small that the Coulombic interaction between charged particles could be neglected. A criterion for treating the plasma as an ideal gas was developed by comparing the Debye-Huckel expression for lowering of the ionization potential for a neutral atom: -

$$\Delta I = \frac{1}{K}e^2/hc$$

and the definition of inverse Debye length

$$1k^2 = 4\pi e^2 \le N_i z_i^2/kTV$$

where Ni/V is the particle density of the i-th charged species. Eliminating  $\chi$ , one gets a measure of the ionic strength

$$\sum_{i}^{8} N_{i}^{2} Z_{i}^{2} / V = (hc)^{2} kT (\Delta I)^{2} / \pi T e^{6}$$
  
=  $4.4369 \times 10^{8} (\Delta I)^{2} T$ 

Assuming that the Coulombic interaction becomes negligible when \$\triangle 1\$ falls below 0.25 cm<sup>-1</sup> and that this occurs below approximately 4000 K, then a reasonable lower limit for the ionic strength of the Debye-Huckel gas is:-

$$\leq N_i z_i^2 / V = 1 \times 10^{11}$$

When the ionic strength was less than  $1\times10^{11}$  particles per cm<sup>3</sup>, the plasma was treated as an ideal gas and the following ionization parameters were not computed: Debye length, ratio of principal quantum numbers for Debye cutoff and Bethe cutoff, and number of particles in the Debye sphere. In the output, these three parameters were set equal to 0.- 19 (i.e.  $0.\times10^{-19}$ ) to indicate untouched computer locations.

For example, for an initial pressure of 0.8 mm Hg and an incident shock velocity of 5 km/sec,  $T_2 = 3680$  K and  $\Delta I = 0.2$  cm<sup>-1</sup>. Therefore

$$\underbrace{\frac{N_{1}z_{1}^{2}}{V}}_{= 0.65 \times 10^{11}} = 4.4369 \times 10^{8} (0.2)^{2} (3680)$$

Since  $\sum_{i} N_{i}z_{i}^{2}/V$  was less than  $1\times10^{11}$ , the gas was considered to be ideal.

OVER-ALL ITERATION PROCEDURE FOR COMPOSITION

The system of equations resulting from minimization of G can not be solved for composition in closed form for two reasons:

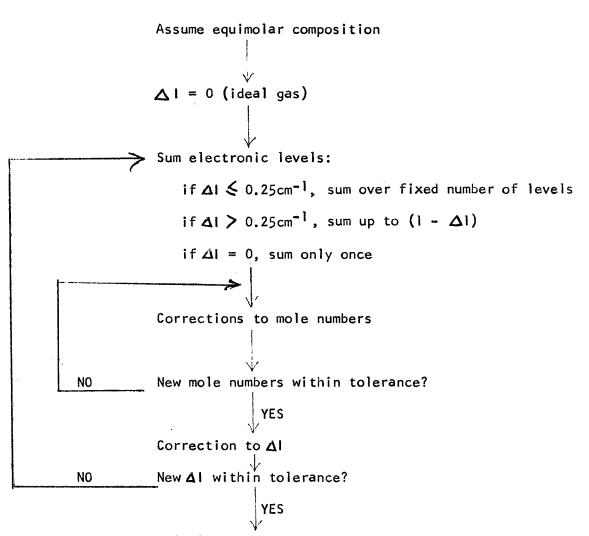
- (1) The system is non-linear in composition; that is, there are terms that contain  $\ln (n_i/n)$
- (2) The electronic partition function of an atomic species with highly excited states depends on the ionic density, which in turn depends on the electronic partition function.

The over-all iteration is accomplished in two stages.

In the first stage, the mixture is initially assumed to consist of equimolar proportions of all species considered. Corrections to these mole numbers and the Lagrangian multipliers are found, assuming that each atomic species has a fixed number of energy levels. These are the observed levels (ref. 11) plus those filled in by the method of reference 9. In this stage, the classical or isolated-atom ionization potential, I, is used. Iteration is terminated when successive estimates of mole numbers agree to five significant figures.

For the second stage, mole numbers from the first stage are used as estimates for a real-gas composition (Debye approximation). These mole numbers are used to calculate an initial estimate of ionization-potential lowering,  $\Delta I$  (ref. 6). When mole numbers have converged for the initial  $\Delta I_{j}$  a new value for this quantity is calculated. Thus, iterations are performed, not only on the mole numbers, but also on  $\Delta I$ .

The following flow diagram summarizes the over-all iteration procedure:-



# Calculate thermodynamic properties

# INCIDENT AND REFLECTED SHOCKS

Calculation of the conditions behind a shock front involves the laws of conservation of mass flow rate (continuity), momentum, and energy. Application of the Newton-Raphson method to these equations results in a set of iteration equations. In reference 12, the independent variables chosen were the logarithm of temperature ratio and the logarithm of pressure ratio across the shock. For use with plasmas, these equations were modified to include the effect of Coulomb compressibility, Z.

# Nomenclature for Shock Parameters

The shock parameters listed in Table I are  $u_1$ ,  $u_2$ ,  $v_2 = u_1 - u_2$ , and  $u_5 + v_2$ .

In order to define these parameters, it will be convenient to refer to Figure 1. The nomenclature is that of reference 13.

# Actual Velocities

Actual velocities are velocities in laboratory-fixed coordinates.

The initial test gas is assumed to be at rest. Therefore, the quantity  $v_1$ , the actual velocity of the gas ahead of the incident shock, is zero.

The quantity  $v_2$  is the actual velocity of the shocked gas behind the incident shock and also the actual velocity of the shocked gas ahead of the reflected shock.

The quantity  $v_5$  is the actual velocity of the shocked gas behind the reflected shock. This velocity is assumed to be zero.

The incident shock velocity is  $\mathbf{W}_{S}$ . The reflected shock velocity is  $\mathbf{W}_{R}$ . Relative Velocities

Relative velocities are velocities relative to the pertinent shock front, i.e. in shock-fixed coordinates.

The quantity  $u_1$  is the relative velocity with which the initial gas flows towards the resting incident shock. Thus

$$u_1 = W_S - v_1 = W_S$$

The quantity  $\mathbf{u}_2$  is the relative velocity with which the shocked gas flows away from the resting incident shock. Thus

$$u_2 = W_S - v_2 = u_1 - v_2$$

and therefore

$$v_2 = u_1 - u_2$$

The quantity  $u_5$  is the relative velocity with which the shocked gas moves away from the resting reflected shock. Thus

$$u_5 = W_R - v_5 = W_R$$

The quantity,  $u_2^*$ , is the relative velocity with which the gas moves toward the resting reflected shock. Thus

$$u_2^* = W_R + v_2 = u_5 + v_2$$

# ATOMIC AND MOLECULAR CONSTANTS

Values for the observed energy levels, statistical weights, and ionization potentials of H, He, He $^+$ , Ne, Ne $^+$ , Ne $^{++}$  and Ne $^{+++}$  were taken from reference 11.

The levels of H were taken to be the same as those for the isoelectronic species He.

The dissociation energies of  $H_2$  and  $H_2^+$  and the electron affinity of H were obtained from reference 14. This publication was also the source for the equations for the partition functions of  $H_2$  and  $H_2^+$ .

# SUMMARY OF RESULTS

The shock relations and associated equations for chemical equilibrium were solved for six entry velocities ( $u_1 = 15$ , 12, 10, 8, 6.5 and 5 km/sec) at six ambient pressures for a simulated Jovian entry atmosphere consisting of 70 percent Ne, 25 percent H<sub>2</sub> and 5 percent He by volume.

The resulting thermodynamic and shock (incident and reflected) properties are presented in Table I. Temperatures and pressures are plotted in Figure 2.

Subtables (a), (b), (c), (d), (e), and (f) of Table I give the properties respectively for initial pressures  $P_1 = 1.0$ , 0.8, 0.4, 0.2, 0.1, and 0.05 mm Hg. These pressures are actually listed in dimensionless form  $P_1/P_0$  where  $P_0 = 760$  mm Hg(1 atmosphere).

Each subtable consists of three parts: properties of the unshocked gas; properties associated with the incident shock; and properties associated with the reflected shock.

The properties given for the unshocked or initial gas are: P/P<sub>o</sub>, T, H/RT, S/R, M, C<sub>p</sub>/R,  $\chi$ <sub>s</sub>, sonic velocity, Mach number, and u<sub>1</sub>.

The properties associated with the incident shock are:  $u_2$ ,  $P/P_o$ , T, H/RT, S/R, M,  $(\partial lnV/\partial lnP)_T$ ,  $(\partial lnV/\partial lnT)_p$ ,  $C_p/R$ ,  $X_s$ ,  $X_s$ , sonic velocity; the Coulombic parameters: ionization potential lowering, Debye length, ratio of Debye principal quantum number to Bethe principal quantum number, number of charged particles in the Debye sphere, and Coulomb compressibility; additional incident-shock properties:  $P_2/P_1$ ,  $T_2/T_1$ ,  $M_2/M_1$ ,  $P_2/P_1$ ,  $V_2 = u_1 - u_2$ ; mole fractions; total particle density; and negative excess thermodynamic properties:

Similar properties are calculated for the reflected shock wave. In this case the ratios are from condition 5 to condition 2 and, instead of  $v_2$ , the velocity  $u_5 + v_2$  is given.

Figure 2(a) gives the temperature and pressure behind the incident shock and Figure 2(b) gives these variables behind the reflected shock. For the conditions of this report, the final temperature increases more rapidly with shock velocity than with initial pressure.

The only shock data available in the literature for the Jovian atmosphere are given in reference 15 for a .50  $H_2$  - .50 He mixture. However, instead of the Debye approximation used in this report, reference 15 used the ideal-gas approximation.

For purposes of comparison, Figure 3 presents two sets of ideal-gas data for this mixture: one calculated by the present author and the other by reference 15. The figure presents theoretical density ratio and temperature for equilibrium states behind incident shocks. There are significant temperature differences between the two calculations: approximately 1000 K at  $u_1 = 42$  672 m/sec (140 000 fps) and approximately 3000 K at  $u_1 = 57912$  m/sec (190 000 fps).

The key to the discrepancies is the following statement in reference 15:

"Since molecular hydrogen is completely dissociated at the temperatures and densities of interest, the only process involving hydrogen is the ionization of atomic hydrogen." This assumption leads to the following errors: (1)

Violation of energy conservation since the dissociation energy of diatomic hydrogen is neglected. (2) Wrong values for molecular weight and thermodynamic properties of the initial mixture.

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# TABLE I. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

(a) P <sub>1</sub> = 1.0 MM Hg						
INTITAL GAS (1)						
P/P(	DEG K	1.3158- 29 C.000 24.373	8 C	MI MOL BT CP/R GAMMA (S) SCN VELIM	2	83221 •7423 •5740 512•9
MACH NO:	29.2460	23.3968	19.4973	15.5979	12.6733	9.7487
UL; MYSEC SHOCKED GAS (2)	15000.00	12C00.C0	10000.00	8000.00	65CC.CO	5000.00
U2, M/SEC	1325.45	1246.82	1196.78		981.75	567.90
L* BEG K b/be	17937	15255	13227	4.3253-1 10856	7753	3714
H/R1 8/R	6.1119 23.1336		4.6596 25.4351			4.8655 25.1200
M, NGL WT	8.16578	9-41016		11.38889		
(DEV/CLF)T	-1.12023	-1.09115	-1.06843	-1.C2463	-1.CC1C9	-1.02067
(CLV/CLT)F CP/R	2.2599	1.9275 16.3416	13.8949	8-2656	1.0216	1:3093 7:1863
GAMMA (S) Gamma	1.1278	1.1577	1.1771	1.2321	1.5313 1.5329	1.2786 1.3050
SON VELIMISEC	4538.4			3124.8		
July Victin Cat	13306.1	3,7012	3,72047	312.00	200047	20001
COUNTRIC FARA	METERS					
IP ECHER, CM-I	809.7	614.5	452.3	247.7	6C.9	0.3
DEBYE LAG, CM DEBN/BEIN	1.434 = 6 8.272 = 1	1.890 -6 8.429 -1	2.568 -6 8.662 -1	4.689 -6 9.268 -1	1.908 -5 1.107 0	019 019
NUMBER EF CHAR						
COUL CEMPRESS	5.129 C C.99325			1.016 1 0.99956		
P2/#1	1228.297	773.083	527.729	328.721	215.615	133.594
T2/T1		51.166		36.411	26.005	12.457 0.8209
M2/M1 RH02/RH01	0.5505 11.3169	C.6344 9.6245	0.7010 8.3557	6.9352	0.7985 6.6208	8.8044
V2±U1-U2,M/SEC	13674.55	10753.18	£803.22	6846.46	5518.25	4432.10
MOLE FRACTIONS						
E				4.0193-2 2.9957-6		
H2 H2+				8.041 -7		
H				3.4387-1		
H+ H-				4.0047-2 8.429 -7		
HE	2.7128-2	3.1677-2	3.5046-2	3.8352-2	3.9925-2	4.1047-2
HE+				1.419 -7 1.80C-27		7.900-24
HE±t NE				5.3735-1		
NF+	9.C03 -2	1.777 -2	2.795 -3	1.459 -4	2.C21 -7	3.828-18
NE++ NE+++		7.578-11 2.343-27		9.851-18 0. C		0. 0
						- 0
PARTICLE CENSI						
TCTAL	6.658 17	4.914 17		2.926 17	2.686 17	3.474 17

2.7005-2 1.5992-2 8.1155-3 1.7594-3 2.8461-5 0.

1.3525-2 8.0040-3 4.0598-3 8.7977-4 1.4223-5 0.

0

0

NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

-(HIBT)CCLL

-(SIR)CCLL

TABLE 1. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25  $\rm{H_2}$  - 0.05 He MIXTURE

	(a) $P_1 = 1.0 \text{ MM Hg}$					
INTTIAL GAS	(1)			THE PERSON NAMED IN COLUMN TWO IS NOT THE PERSON NAMED IN COLUMN TO THE PERSON NAMED IN COLUMN T		
P,	'P0	1.3158-3	My MOL BY	14.83221		
	TO EC K	298	CP/R	2.7423		
57	'R <b>1</b> 'R	€.000€ 24.373€	GAMMA (\$)	1.5740		
PACH NO.	29.2460		SEN VEL + M 9.4973 15.5975	7SEC 512.9 12.6733 9.7487		
UI A MYSEC		12C00.C0 1C		65CC.CO 5CCO.CO		
1	- Harrison . U.A.					
SHOCKED GAS (5				1/0/ 00 1//2 2/		
U5→ M/SEC P/P€	2605 <b>.</b> 92		392.81 1757.12 3885 0 3.6486 0	1684.C9 1642.34 2.3554 0 2.0419 0		
T, BEC K	29424	22092	19196 16092			
H/RT	6.1392		5.5906 4.8683			
\$/R	19.7480	21.1153 2	2.2939 23.6574	24.6530 24.9758		
M, NEL ST	6.23848	7.47472 8	.52233 9.74969	10.74653 11.58835		
(DLV/CLF)T		-1.15855 -1	.14456 -1.1C160	-1.C6258 -1.01644		
(CLV/CLT)F	1.3752		2.1794 1.8571			
CP/R GANNA (S)	6.1637 1.3270		9.3644 14.7739 1.1120 1.1519			
GANNA	1.4072	1.2960	1.2728 1.2689			
SON VELAM/SEC	7213.8	5243.1	4563.4 3975.8	3549.1 3210.6		
COLLEMBIC FARA	METERS			•		
IP MEWER, CM-1	2230.7	1914.6	1487.7 1024.9	702.0 401.4		
DEBYE LNG, CM				1.6521-6 2.8933-6		
DEBNIBETN	7.5855-1	7.4199-1 7.	5595-1 7.8107-1	8.0960-1 8.5833-1		
NUMBER OF CHAF	CEC PARTIO	CLES IN DEBY	SPHERE			
COUL COMPRESS				4.5099 0 6.3957 0 0.99768 0.99959		
COOR CEPPRESS	U + 70214	0.70402 0	190922 C 49422	0.44100 0.44434		
P5/#2	13.273	11.255	9.920 8.436			
T5/T2 M5/M2	1:640 0:7640	1.448 C.7943	1.451 1.482 0.8196 0.8561	1.766 2.990 C.9C74 0.9517		
RH05/RH02	6.2475		6.6509 4.8964			
U5+W2 +M/ SEC	16280.46	12803.38 10	96.03 8603.58			
MOLE FRACTIONS						
E				9.4332-2 2.3396-2		
H2 H2+				3.3225-6 1.4367-5 3.5906-6 2.1777-6		
H				2.7029-1 3.6731-1		
H+				9.1965-2 2.3298-2		
H- HE				3.9807-6 2.2960-6		
enc HE≢.				3.6223-2 3.9065-2 4.4758-6 1.0234-7		
HE++	3.262 -8	3.884-12 2.	73-14 8.698-18	1.636-21 1.847-27		
NE	2.7926-2	1.8839-1 3.	325-1 4.4354-1	5.0482-1 5.4681-1		
NE+ NE++				2.3629-3 9.7904-5 2.122-13 6.050-18		
NE+++			044-21 1.916-26			
•		- · · ·				
DADTICUT CCSCS	11EC 3/655	. 4.7				
PARTICLE CENSI	11ES,1/UM	** <b>5</b>	and the second s	والمتعادية المتعادية والمتعادية والمتعادية والمتعادية والمتعاد والمتعادية وال		

TCTAL 5.445 18 3.863 18 2.662 18 1.673 18 1.266 18 1.350 18

#### NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

-(HIRT)CCLL 6.9046-2 6.1524-2 4.1895-2 2.1791-2 9.2937-3 1.6224-3 -(SIF)CCLL 3.4674-2 3.0882-2 2.1003-2 1.0911-2 4.6495-3 8.1129-4

TABLE 1. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25  $\rm H_2$  - 0.05 He MIXTURE

(b) $P_1 = 0.8 \text{ MM Hg}$						
INITIAL CAS (1	)					
P/P	₿	1.0526-3 298		My NOE BT		3221
'! i J H/R'	T Deg-k	0.0000		CP/R GAMMA (S)		.7423 .5740
5/R	•	24.5968		SEN VELIM		512.19
MACH NO.	29.246C	23.3968	19.4973	15.5979	12.6733	9.7487
UL; MYSEC	15000.00	12000.00 1	00.000	8000.00	65CC.CO	5CC0.00
SHOCKED CAS (2						F / 0 0 F
U2 / M/SEC P/PE	1310.75	1234.10 8.1473-1 5		1143.54		
T'S BEG K	17797	15066	13670		7741	3680
H/RT	6.1780	5.3350	4.7069		3.7983	4.9039
S/R	23.3029	24.5472	25.6029	26.5061	26.41C1	25.3015
MA NOL BT	8.14718	9.38066 1	10.37519	11.37302	11.84138	12.15613
(DEN/CLP)T		-1.08887 -				
(DEA/CEA)b	2.2614		1.7584		1.0237	1.2965
CPZR GANMA (S)	22.1850 1.1283	16.4687 1.1596	14.2022		3.C483 1.5212	7.0300 1.2812
GANMA	1.2601	1.2626	1.2561		1.5230	1.3063
SON VELIMISEC	4515.15	3935.0	3509.9	3108.5		1795.6
EXCEPTION OF THE CANADA STREET, THE CANADA STREET, CO.		3-11-11-1	······································			
COUNCERS FARA	METERS					
IP LCWER, CN-1	73547	540 1	412.8	227.3	E7 1	0.3
DEBYE LNG CH		2.074 -6 2	412.0 6- 813.5	5.109 -6	2.033 -5	0.2
DEBN/BETM		8.544 -1 8				
NUMBER OF CHAR	GEC PARTI	CLES IN DEE	YE SPHE	RE		
	5.574 C	6.226 0 7	7.316 0	1.098 1	2 125 1	019
COUL CEMPRÉSS	C.99376		0.99810		0.99999	
P2%P1	12291617	773.996	528.524	329.198	215.679	133.743
T2/T1	59.391	50.531	43.838		25.964	12.341
M2YM1	C.5493	C.6325	0.6995		0.7984	0.8196
RH02/RH€1 V2±U1-U2,M/SEC	11.4438	9.7237	8.4495		6.6320	8.8818
V2-61-62,6/3EC	13009.23	10102.90	8816.50	6856.46	5519.90	4437.05
MOLE FRACTIONS						
c	3 1220-1	2 (0/4-1 1	2542-1	A. 1521 C	2 0724 2	1 2014 0
E H2		2.0944-1 1 1.5610-7 6				
H2+		8.626 -7 1				
H	5.1359-2	1.2402-1 2	2.2677-1	3.4199-1	3.97C7-1	3.6085-1
H+		1.9221-1 1				
H- HE		1.021 -6 1 3.1580-2 3				
HE+	3.883 -4	4.248 -5 4	.440 -6	1.329 -7	5.899-11	
HE#4	4.269-15	1.427-18 4	.243-22	1.200-27	0. 0	0. 0
NE NE≠		4.2553-1 4				
NE+4		1.719 -2 2 5.852-11 1				
NE+++		1.188-27 2				0. 0
PARTICLE CENSI	TIES,1/CM	<b>*</b> *3				
TGTAL	5.399 17	3.584 17 3	.130 17	2.364 17	2.153 17	2.808 17
NEGATIVE EXCES	E THERMOC'	YNAMIC PROP	ERTIES			

2.4978-2 1.4937-2 7.6115-3 1.6829-3 2.9355-5 0.

1.2508-2 7.4755-3 3.8076-3 8.4154-4 1.4670-5 0.

-(RARI)CELL

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TABLE I. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS
THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H <sub>2</sub> - 0.05 He MIXTURE						
		(b) P <sub>1</sub> = 0.8 MM Hg				
INITIAL GA	5 (1)					
	P7P0	1.0526-3 298	M, NOL WT	14,83221		
	T: DEG K H/RT	C • 000 C	CP/R GAMMA (S)	2.7423 1.5740		
	S/R	24.5968	SEN VELINA			
MACH NO.	29.246			12,6733 9,7487		
U1, M/SEC	15000.00	0 12000.00 10000.00	0.000°C	65CC.CO 5CCO.CO		
		TECEQUILIERIUM				
U5; M/SEC P/P6	2586.09 1.7353 1		1740.23	1665.C8 1630.76 1.8837 0 1.6469 0		
T, DEG K	29058			13516 11021		
H/RT	6.1922			4.3034 3.7170		
S/R	19.8768	21.2414 22.4276	23.7970	24.8291 25.1640		
MS MCL WT	6.21422			10.72592 11.57701		
#DUN/CLP)T #DUN/CLT)P		-1.15338 -1.13984 2.2520 2.1862		-1.06186 -1.01676		
CPYR	6.0678			1.5976 1.1980 11.5929 5.9834		
GAMMA (S)	1.3311					
GANMA	1.4053	1.2949 1.2714	1.2692	1.1881 1.2872 1.2616 1.3088		
SON VET /M/SE		5226.6 4548.7	3961.5	3527.5 3191.9		
CCUTCWBIC by						
IP MER, CN-	1 2034.17		938.5	641.3 370.6		
DEBYE LNG,CM Debn/eetn				1.811C-6 3.1341-6 8.2C36-1 8.6860-1		
•				0.2030 1 0.0000 1		
NUMBER EF CF	ARGEL PARTIG	CLES IN DEBYE SPHE	RE			
				4.8821 0 6.8565 0		
COUL COMPRES	S 0.98399	0.98566 0.99021	0.99488	0.99782 0.99961		
P5/#2 T5/12	13.407 1.641			8.297 11.698 1.746 2.995		
M5/M2	C.7627		0.8547	0.9061 0.9524		
RHOS/RHE2	6.2934		4.9400	4.3151 3.7209		
U5+V2+NZSEC	16275.34	12797.39 10691.87	8596.69	7184.58 6067.81		
MOUE FRACTIC	N S					
E	4.7629÷1	3.7246-1 2.8419-1	1.8082-1	9.5731-2 2.4349-2		
H2	1.2572-9	4.8685-8 1.7697-7	7.9267-7	2.7609-6 1.1960-5		
H2+ H				3.0164-6 1.8713-6 2.6819-1 3.6598-1		
H+				9.3508-2 2.4253-2		
H-				3.3344-6 1.9691-6		
HE HE≠				3.6167-2 3.9026-2 4.0690-6 9.7851-8		
HE++	2.579 -8	3.009-12 1.531-14	5.821-18	9.718-22 1.337-27		
NE	2.5856→2	1.8677-1 3.2254-1	4.4271-1	5.0417-1 5.4628-1		
NE+ NE++				2.2193-3 9.5871-5 1.505-13 4.985-18		
NE+++		1.189-17 3.085-21				
				-		
PARTICLE CEN	SITIES, 1/CM	<b>* *</b> 3				
TCTAL	4.454 18	3.162 18 2.180 18	1.366 18	1.025 18 1.097 18		

6.4045-2 5.7370-2 3.9152-2 2.0485-2 8.7138-3 1.5707-3

3.2152-2 2.6789-2 1.9624-2 1.0256-2 4.3592-3 7.8540-4

NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

-(HIRT)CCLL

-(SIR)CELL

TABLE 1. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

		(c) P <sub>1</sub> :	= 0.4 MM Hg			
INITIAL CAS (1	and the contract of the contract of					T 12 1 - 1 - 1 - 1 - 1
P/P	C	5.2632-	<del>-</del> 4	M' NOL WI	14.	83221
	DEG K		3.6	CP/R		.7423
H/R	1	0.000		GANMA (S)		.574C
\$/R		25.289	99	SCN VELAN		512.9
MACH NO.	29.246C	23.3968				
U1 / M/SEC SHOOKED GAS (2		12C00.C0	10000.00	800C.CC	65CC.CO	5000.00
U2. M/SEC	1269.76	1193.31	1144.05	1112.06	974.12	548.48
P/P6				1.7406-1		
T. DEG K	17037		12600		7697	3579
H/RT	6.3704				3.8186	5.0204
S/R	23.7927	25.0357	26.1163		27.0852	25.8717
67 K	2361721	23.000	20.1103	2100004	21.0032	2340111
My MCL WT	8.07840			11.32525		
(DLV/CLP)T	-1.10697	-1.08210	-1.06652	-1.02619	-1.CC151	-1.01640
(DEV/CLT)F	2.2717	1.9301	1.8044	1.3806	1.0314	1.2545
CP/R	23.1245	16.7724	15.1627	9.3746	3.2290	6.4899
GA™MA (S)	1.1315	1.1628	1.1740	1.2152	1.4880	1.2921
GAMMA	1.2525	1.2583	1.2521	1.2471	1.4902	1.3133
SON VELIMISEC	4454.2	3880.7	3454.8	3056.2	2836.7	1782.8
COULCMBIC FARA	METERS					
IP UCHER, CP-1	546.11			173.5		0.1
DEBYE LAC, CA	2.127 -6			6.695 -6		
DEBN/BETN	8.758 -1	8.911 -1	9.149 -1	9.786 -1	1.156 0	019
NUMBER OF CHARG	EC PARTIC	CLES IN DE	ERYE SPHE	RE	nen <del>n e der</del> im die <u>en den</u>	an ing paggarang dari dari dari dari dari dari dari dari
	7 220 C	8 • C 17 C	0 301 A	1:424 1	3.8C9 1	019
COUR COMPRESS	C.99509		0.99844		0.99999	
P2/#1	1233.305	776.925	530.884	330.705	215.912	134.175
T2/11	57.142	48.610	42.259		25.816	12.005
M2/M1	0.5447		0.6947		0.7578	0.8156
RHC2/RHO1	11.8133	10.0561	8.7409			9.1162
V2=U1-U2,M/SEC					5525.88	4451.52
NO. 5 - 5046716W6						
MOLE FRACTIONS						
E	3.1918-1	2.1588-1	1.3162-1	4.5555-2	2.7377-3	9.6888-9
H2				1.3979-6		
H2+				4.091 -7		
Н				3-3634-1		
H+				4.5432-2		
H <del></del>				4.245 -7		
HE				3.8178-2		
HE∌				1.06C -7		
HE#4				3.138-28		0. 0
NE				5.3437-1		
NE≠				1.227 -4		
NE++				3.151-18		
NE+4-1		1.341-28				0. 0
111, 777	0.111_53	10341-50	¥ •02134	<b>.</b> .	<b>.</b>	0
PARTICLE CENSI	14ES.1/0N:	<b>*</b> *3				
TOTAL			1.630 17	1.221 17	1.084 17	1.448 17
NEGATIVE EXCES	S THERMOD	YNAMIC PRO	OPERTIES			

-(H/RT)CCLL 1.9627-2 1.1962-2 6.2245-3 1.4460-3 3.1886-5 0. -(S/R)CCLL 9.8257-3 5.9854-3 3.1135-3 7.24C5-4 1.5944-5 0.

TABLE 1. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

(c)  $P_1 = 0.4 \text{ MM Hg}$ 

			The state of the s	
INITIAL CAS (		بهادونا والوارات		The same
P/P	DDEG K	5•2632 <del>-</del> 4 298	MI POL WT	14.83221
H/R		C.0000	CP/R	2.7423
5/8		25.2899	CAMMA (S) SCN VELIMA	1.5740 SEC 512.9
MACH NO.	29.246C	23.3968 19	.4973 15.5979	12.6733 9.7487
U14 M/SEC		12000.00 100		
SHOOKED GAS (5				
U5; M/SEC	2521.52		820.01 1685.11	1609.46 1594.42
P/P0		4.7801 0 2.8	8820 0 1.5118 C	9.4217-1 8.4326-1
T, DEG K	27994	20888	18218 15279	
H/RT S/R	6.3641 20.3350		5.8189	
3/1	26.5550	21.71.70 2.	2.0000 24.2000	20.5000 20.1400
M', MCL WT	6.15697	7.38783 E	.41945 9.6444C	10.67449 11.54110
(DLV/CLP)T				-1.06018 -1.01774
(DLV/CLT)F	1.3113		2.1994 1.8881	
CP/R GAMMA (§)	5.7521 1.3419		0.4035 15.5169 1.1239 1.1592	
GANNA	1.4011		1.2665 1.2663	
SON VELIMISEC	7122.2		4496.6 39C7.5	3465.2 3136.4
CCLUCKPIC FARA	METERS			
IP LOWER, CN-1	1521.7	1318.7	1028.C 711.4	482.5 288.0
DEBYE LNG CM				2.4068-6 4.0320-6
DEBN/BETN				8.5470-1 9.0218-1
NUMBER OF CHAR	CEC PARTI	CLES IN DEBY	E SPHERE	
				·
COUR COMERCE				6.2435 0 8.6093 0
CCUL CCMFRESS	. 0.90145	U.90001 U	.99214 0.99582	0.99821 0.99965
P52 <b>P</b> 2 T5/T2	13.789		10.314 8.686	
M5/M2	1.643 C.7622		1.446 1.459 0.8171 0.8516	
RHOS/RHO2	6.4452		5.8659 5.C875	
U5+V2+M2SEC		12773.18 10		
MOLE FRACTIONS				
E				1.0040-1 2.7370-2
H2				1.555 -6 6.791 -6
H2+ H				1.7568-6 1.1617-6 2.6126-1 3.6176-1
H+				9.8571-2 2.7282-2
H-				1.9254-6 1.2146-6
HE				3.5981-2 3.8905-2
HE+				3.0264-6 8.3482-8
₩E#4				1.932-22 4.548-28
NE +				5.0195-1 5.4459-1 1.8265-3 8.8393-5
NE++				5.193-14 2.585-18
NE+++			703-22 1.191-27	
PARTICLE CENSI				<u>and the second of the second </u>
TOTAL	2.376 18	1.699 18 1.	170 18 7.293 17	5.326 17 5.756 17
NEGATIVE EXCES	S THERMOC	YNAMIC PROPE	RTIES	

5.C216-2 4.5705-2 3.1443-2 1.6722-2 7.1453-3 1.4061-3 2.5188-2 2.2918-2 1.5753-2 8.37C0-3 3.5742-3 7.0313-4

- (HIRT)CCLL - (SIR)CCLL

TABLE I. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

	THROUGH A	0./0 Ne - C	J. 25 H2 - U.	US HE MIXIU	KE	
(d) $P_1 = 0.2 \text{ MM Hg}$						
INITIAL CAS (1	)				1	
	P <b>0</b>	2.631	5-4	M; MCL I	1 14	83221
	ZDEG R		298	CP/R		2.7423
H/ 6/		C • 00 25 • 98		GANMA 15		1.5740
MACH NO:				SON VEL		512.9
U1; MYEEC	29.2460	23.3968		15.5979 8000.00	12.6733 6500.00	9.7487 5000.00
SHOCKED GAS 12			1000000		0,000,00	3000.00
U2; M/SEC	1231.39	1155.27	1105.87	1081.24	966.76	535.44
P/P0		2.C517-1				
T' DEG K	16415	13955	12149 5.0060	10181	7643	3489
H/R <b>T</b> S/R	6.5601 24.2838	5.6731 25.5167		4.1856 27.6636	3.8438 27.7557	5.1307 26.4525
	2		20002,0			220.020
M. MOL ET	8.01212		10.23727			
(DLV/CLF)T (DLV/CLT)F	2.2839	-1.07587 1.9240	1.8483	1.4227	1.00193	1.2107
CP/R	24.0777				3.4570	5.8838
GAMMA (S)	1.1337		1.1709	1.2041	1.4526	113087
GAMMA	1.2456	1.2541 3828.5		1.2371	1.4554 2794.0	1,3261
SON VELIMISEC	4394.3	3020.9	2244.0	3006.2	2194.0	1775.4
CCLUCMBIC FARA	METERS					
				•		
IP UCHER, CM-1	404.16	312.5	233.0	131.9	38.0	0.1
DEBYE LNG, CM	2.870 -6	3.717 -6	4.983 -6			
DEBMISEIN	9.152 -1	9.297 -1	9.540 -1	1.019 C	1.195 0	019
NUMBER OF CHAR	GEC PARTIO	CLES IN DI	EBYE SPHEI	RE		
COUL CCMFRESS	9.441 C C.99616	1.035 1				
COUR CUPPRESS	C*33016	0.99761	0.99814	0.99969	0.55559	1.00000
P2/R1	1236.740	779.661	533.171	332.180	216.198	134.566
12/11	55.055	46.806	40.747	34.146	25.633	11.703
M2/M1	0.5402	0.6221	0.6902	0.7603	0.7572	0.8122
RHC2/RHO1 V2≠W1+U2,M/SEC	12.1813	10.3872		7.3989 6918.76	6.7235 5533.24	9.3382 4464.56
, , , , , , , , , , , , , , , , , , , ,	13.00001	100	2071113	0710110	2220624	4404630
MOLE FRACTIONS						
E	3.2477-1	2.2238-1	1.3724-1	4.9580-2	3.5574-3	7.5773-9
H2	3.0908-9	3.6733-8	2.0408-7	7.9064-7	4.5527-6	1.5190-2
H2+		2.476 -7				
H H+		1.0242-1				
H-	1.279 -7	2.857 -7	3.914 -7	2.5C7 -7	3.839 -8	1.385-12
HE	2.6675 → 2	3.1077-2	3.4508-2	3.8017-2	3.9858-2	4.0608-2
HE++		2.803 -5 1.035-19				
NE NE		4.2174-1				0. 0 5.6851-1
NE+	8.964 -2	1.373 -2	1.811 -3	1.052 -4	3.214 -7	3.895-19
NE++	7.419 -9	1.029-11	1.396-14	1.161-18	6.444-27	0. 0
NE#+€	1.866-23	1.454-29	1.268-35	U* C	C. 0	0. 0
PARTICLE CENSI			<u> </u>		. E	
TCTAL	1.461 17	1.082 17	8.487 16	6.304 16	5.464 16	7.449 16

### NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

1.5358-2 9.5522-3 5.0507-3 1.2321-3 3.3915-5 0. 7.6865-3 4.7789-3 2.5261-3 6.1607-4 1.6958-5 0. -{H#RT}@CLL 0 -(SIR)CELL

TABLE I. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

	THROUGH A	0.70 Ne - 0.25 H <sub>2</sub> - 0.0	05 He MIXTURE			
(d) $P_1 = 0.2 \text{ MM Hg}$						
INITIAL GAS	111					
THITTE GES	P/P0	?.6316-4	M; MCL DT 1	4.83221		
	T, DEG K	298	CP/R	2.7423		
	H/RT	C.0000	GANMA (S)	1.5740		
	S/R	25.9830	SCN VELIMISEC	512.9		
MACH NO.	29.246 15000.0	0 23.3968 19.4973 C 12000.00 10000.00				
	**************************************	TECEQUILIBRIUM				
U5, M/SEC	2461.23	1908.65 1768.76	1632.71 1556.4	2 1556.97		
P/P0		2.4672 0 1.4906 0				
Ty DEG K	27059 6.5296	20054 17535				
H/R1 S/R	20.8264	6.6206 5.9896 22.1574 23.3203				
37 K	20.0201	2241511 2545203	2101331 230701			
M, NEL RT	6.11021	7.31807 8.34210				
(DLV/CLP)T		-1.12809 -1.11527				
(DLV/CLT)F CP/R	1.2635 5.3698					
GAMMA (S)	1.3559					
GAPMA	1.4031	1.2818 1.2608	1.2634 1.251	5 1,2765		
SON VELIMISEC	7065.6	5087.9 4444.9	3854.0 3404.	3 3081.2		
COULEMBIC PAR	AFETERS					
IP HOWER, CM-1	1133 aC	993.3 776.1	538.6 362.	7 222.4		
DEBYE LAG, CM		1.1693-6 1.4964-6				
DEBN/PETN	8.3740-1	8.1452-1 8.2989-1	8.5647-1 8.9074-	1 9.3767-1		
NUMBER OF CHAI	RCEC PARTI	CLES IN DEBYE SPHE	RE			
	5.5263 C	4.6783 0 5.2305 0	6.3222 C 7.9999	0 1.0820 1		
COUL COMPRESS	0.99025	0.99090 0.99370	0.99660 0.9985	4 0.99969		
P5/#2	14.169	12.025 10.624	8.885 8.29	9 12.162		
T5/12	1.648	1.437 1.443				
M5/M2	C.7626	0.8149				
RHC5/RHC2	6.5942					
U5+V2 + M/ SEC	16229.83	12753.38 10662.90	8551.47 7089.6	6 6021.53		
MELS EDACTION	c					
MOLE FRACTION	3					
E		3.8326-1 2.9696-1				
H2		8.038 -9 3.424 -8				
H2+ H		2.7507-7 5.2978-7 3.1626-2 6.0265-2				
п Н+		2.1507-1 2.2095-1				
H-		5.3193-7 7.7457-7				
HE	7.1206-3	2.3367-2 2.7816-2	2 3.2231-2 3.5799-	2 3.8786-2		
HE+		1.3025-3 3.0559-4				
HE++		6.076-13 2.363-15				
NE NE+		1.7848-1 3.1799-1 1.6689-1 7.5707-2				
NE++		5.832 -7 1.286 -8				
NE+++		8.255-19 1.437-22				
PARTICLE CENS		<b>*</b> *3				
CLASSICE CENS	PARTICLE CENSITIES,1/CM**3					

TCTAL 1.263 18 9.113 17 6.279 17 3.891 17 2.771 17 3.016 17

### NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

-(H/RT)@CLL 3.8996+2 3.6417-2 2.5215-2 1.36C1-2 5.83C9-3 1.2352-3 -(\$/R)@CLL 1.9546-2 1.8250-2 1.2627-2 6.8064-3 2.9165-3 6.1764-4

TABLE I. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

(e) P	, =	0.1	MM	Нg
-------	-----	-----	----	----

(e) $P_{l} = 0.1 \text{ MM Hg}$						
INITIAL CAS (1	1					
	PC ·	1.315		M. MOL I	1 ال	83221
	10 EG K	C • 00	298 nac	CP/R GAMMA (S	: 1	2.7423 1.5745
\$/		26.6			M/SEC	512.5
MACH NO.	29.2460		19.4973			9.7487
U1; M/SEC		12C00.C0	10000.00	8000.00	6500.00	
SHECKEE CAS 12						
\2, M/SEC P/P€	1194.07	1118.45 1.0293-1	1069.06	1051.03	957.96	523.89
I DEC K	15833	13446	11718		7578	3410
H/R1	6.7553	5.8460	5.1622		3.8746	5.2326
\$/R	24 • 7985	26.0116	27:1659	28.2400	28.4210	27.0450
M. MCL BT	7.95484	9.15691	16.17492	11.23052	11.81152	12.00078
(DLV/CLF)T	-	-1.07007				
(CLV/CLT)F	2.2961	1.9090		1.4658	1.0527	1.1671
CP/R GAMMA (S)	25.1115 1.1337	17.0798	17.2008 1.1674	11.2431 1.1940	3.7378 1.4166	5.2410 1.3326
GAMMA	1.238C	1.2491		1.2282	1.4200	
SEN VELIMISEC	4331.3		3343.3	2957.9		
CCLUCMBIC FARA	* ETERS					
10 11511/10 51 1	200.11	536 7			26 (	
IP UCWER, CN-1 DEBYE LNC, CM	299.11	4.992 -6		59.5 1.162 -5		
DEBN/BETN		9.711 -1				
NUMBER OF CHAR	CEL PARIIL	CLES IN LI	FRAF 256F)	₹		•
	1.227 1					019
COUL COMFRESS	C.59701	0.59811	C•99898	0.95974	0.99999	1.00000
P2/F1	1240.088			333.626	216.540	134.916
T2/11	53.103			33.196	25.415	11.438
M2/M1 RHC2/RF01	C.5363 12.5620		0.6860 9.3540	0.7572 7.6116	C.7964 6.7852	0.8091 9.5440
V2=U1-L2,M/SEC						
MOLE FRACTIONS						
E	3.2960-1	2.2829-1	1.4250-1	5.3537-2	4.54C6-3	6.1988-9
<b>H</b> 2	1.1771-9	1.7675-8	1.1305-7	4.4923-7	2.4105-6	1.1378-2
H2+		1.311 -7				
H H+		9.2592-2 2.1609-1				
H		1.495 -7				
HE	2.6504-2	3.C846-2	3.4298-2	3.7858-2	3.9818-2	4.C455-2
HE+	3.123 -4	2.256 -5	1.816 -6	6.33C -8	9.066-11	
HE++ NF	2.8523-1	2.660-20 4.1998-1	4.7873-1	1.685-25	C. 0	0. 0
NE+		1.218 -2				
NE++	4.587 -9	4.419-12	4.686-15	4.396-19	6.657-27	0. C
NE+++	3.961-24	1.489-30	7.967-37	c •	0 • 0	0. 0
PARTICLE CENSI	TIES,1/CM	**3				
TCTAL	7.587 16	5.629 16	4.417 16	3.256 16	2.76C 16	3.821 16
NEGATIVE EXCES	: THERMOE	YNAMIC PRI	CPERTIES			

1.1945-2 7.5781-3 4.069C-3 1.0365-2 3.5197-5 0. 5.9770-3 3.7909-3 2.0350-3 5.1827-4 1.7591-5 0.

0 0

-(HIRT)CCLL -(SIR)CCLL

TABLE 1. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

(e) P<sub>1</sub> = 0.1 MM Hg

		(e) $P_1 = 0.1 \text{ MM H}$	9	
INTIAL CAS I	1)			
Р	/P0	1.3158-4	M, NOL WT	14.83221
	* DEG R	298	CP/R	2.7423
	/R1 /R	(.000C	GAMMA (S)	1.574C 512.5
MACH NO.		26.6762	SCN VELIMISEC 15.5979 12.6	and the second s
U14 M/SEC	29.2460 15000.00	23.3968 19.4973 12C00.CC 1CC0C.CC		
	•			200000
US, MYSEC	2406.58	EDEQUILIPRIUM 1848.36 1717.21	1582.79 150	5.18 1519.16
P/P€		1.2730 0 7.7077-1		
T, BEG K	26254	19266 16891		2067 10210
H/RT	6.6858	6.8368 6.1688		6739 3.9430
S/R	21.3497	22.6516 23.7937	25.2036 26.	4418 26.9076
M, MOL WT	6.07283	7.26754 8.27839	9.49688 10.5	6957 11.47067
(CLV/CLP)T		-1.11845 -1.10528		
(CLV/CLT)F	1.2180	2.3105 2.2111		7282 1.2882
CP/R	4.9648			2070 7.8176
GAMMA (S)	1.3722 1.4100			1777 1.2387 2459 1.2629
GAMMA SCN: VELIM/SEC	7023 dC	5008.9 4384.9	3801.1 33	43.5 3027.7
3011 100 111 000	.02343	207007	300202	
COULOMBIC FARA	NETERS			
IP MOWER, CM-1	840.1	746.0 584.2	407.2 2	72.1 170.7
DEBYE LNG.CM		1.5568-6 1.9880-6		
DEBNIBETN		8.4867-1 8.6466-1		
NUMBER OF CHAR	GEC PARTIO	CLES IN DEB <b>Y</b> E SPHE	RE	
COLU COMERTE		5.9892 0 6.6861 0		
COLE COMPRESS	C.9925C	0.99280 0.99498	0.99725 0.9	·5882 · 0 • 99973
P5/#2 T5/12	14.567	12.367 10.942		2.323 12.358
M5/M2	1.658 0.7634	1.433 1.441 C.7937 0.8136		L•592 2•994 .8948 0•9558
RHCE/RHO2	6.7367	6.8871 6.2008		6820 3.9464
U5+12,M1SEC	16212.51	12729.92 10648.15		7.22 5995.27
MCLE FRACTIONS				
E	4.9821-1	3.8752-1 3.0233-1	1.9964-1 1.09	3.3300-2
H2	2.750-11	3.193 -9 1.468 -8	1.119 -7 5.00	9 -7 2.233 -6
H2+		1.3250-7 2.6795-7		
H H+		2.6539-2 5.1537-2 2.1845-1 2.2753-1		
H-		2.5529-7 3.8739-7		
HE		2.3259-2 2.7628-2		
HE+	1.4452-2	1.2399-3 2.7878-4	2.3020-5 1.60	76-6 5.4843-8
HE++		2.697-13 9.199-16		
NE NE+		1.7516-1 3.1617-1 1.6783-1 7.4522-2		
NE++		3.714 -7 7.522 -9		
NE+++		2.080-19 2.990-23		
PARTICLE CENSITIES,1/CM**3				
TCTAL		4.885 17 3.366 17	7 2.076 17 1.4	44 17 1.578 17
		<del>-</del> -		_

2.9996-2 2.6787-2 2.0060-2 1.1019-2 4.7258-3 1.0682-3 1.5026-2 1.4419-2 1.0043-2 5.5132-3 2.3636-3 5.3412-4

NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

-(HIRT)CCLL -(SIR)CCLL

TABLE 1. CONTINUED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A 0.70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

(f)  $P_1 \approx 0.05 \text{ MM Hg}$ 

		(f) P <sub>1</sub> =	= 0.05 MM Hg			
INITIAL GAS (1)				<del></del>	···	
P/1		6.5789	)-5	M. NCL W	T 14	.83221
Τ,	DEG K	2	9.8	CP/P		2.7423
H/F		C • 00		GANNA (S		1.5740
\$/F	₹	27.36	93	SON VEL;	M/SEC	512.9
MACH NO!	29.246C	23.3968	19.4973	15.5979	12.6733	9.7487
U1, M/SEC	15000.0C	12000.00	10000.00	3000.00	6500,C0	5000.00
SHOOKED GAS (5		NΤ				
UZ, M/SEC	1158.75	1083.55		1021.56	947.71	514.05
P/PE			3.5358-2			
T, GEG K H/RT	15289	12968	11311	9621	7502	3343
5/R	6.9508 25.3200	€.0207 2€.5109		4.4015	3.9112	5.3236
3/16	25.5200	26.5109	27.6899	28.8164	29.CE10	27.6505
M. HCL BT	7.90112	9.08990	10.11265	11.18469	11.75831	11.96232
(DLV/ELF)T			-1.06364			
(DLW/CLT)P	2.3117	1.9876		1.5096	1.0666	1.1254
CP/R	26.2292	17:0694	18.2545	12.2638	4.C753	4.5971
GAMMA (S)	1.1329	1.1684		1.1849	1.3815	1.3660
GAMMA	1.2308			1.2202	1.3856	
SON VELIMISEC	4269.3	3722.8	3290.5	2911.0	2702.4	1781.5
CCLEOMBIC FARA	NETERS					
IP LOWER, CF-1	220:7			75.4	24.5	0.0
DEBYE LNC , CM			8.91C -6			
DEEN/BETN	1.000 0	1.014 0	1.039 0	1.107 C	1.281 0	019
NUMBER OF CHAR	GEC PARTI	CLES IN C	EBYE SPHEE	₹E		
			2.021 1			
CCUL CEMPRESS	C.99769	0.99850	C.99918	0.99978	C.55559	1.00000
P2/F1	1243.259	784.806	537.441	335.037	216.939	135.208
T2/11	51.280	43.494	37.937	32.268	25.160	11.211
M2/M1 RH02/RHQ1	C.5327 12.9450	C.6128	0.6818 9.6669	0.7541 7.8312	0.7955 6.8586	C-8065 9.7267
V2=U1-L2,M/SEC			8965.54	6978.44	5552.29	4485.95
MCLE FRACTIONS						
E	3.3412-1	2.3394-1	1.4775-1	5.7399-2	5.6869-3	5.3855-9
H2			6.284 -8			
H2+			1.171 -7			
H			1.9434-1			
H+			1.4656-1			
H-			1.245 -7			
HE	2.6342-2	3.0624-2	3.4089-2	3.7704-2	3.9773-2	4.0325-2
HE+			1.315 -6			
HE++			6.373-25			0. 0
NE+			4.7608-1 1.186 -3			
NE++			1.530-15			
NE+++			4.718-38			0. 0
PARTICLE CENSI	11ES,1/CM	<b>*</b> *3				
TCTAL	3.936 16	2.927 16	2.296 16	1.682 16	1.39€ 16	1.953 16
					, -	

9.2536-3 5.9849-3 3.2664-3 8.6290-4 3.5614-5 0. 4.6295-3 2.9935-3 1.6335-3 4.3146-4 1.7799-5 0.

NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

- (H/RT)CCLL - (S/R)CCLL

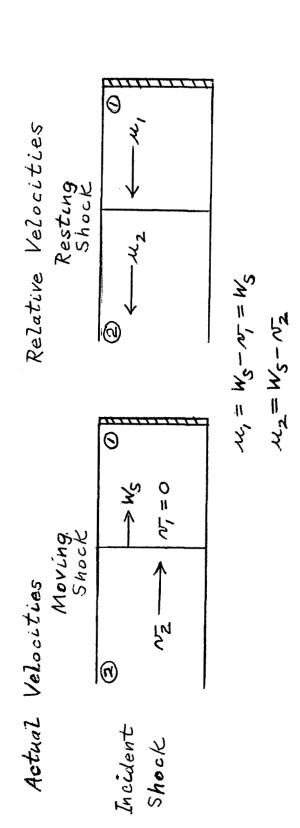
TABLE 1. CONCLUDED. THERMODYNAMIC PROPERTIES FOR EQUILIBRIUM STATES BEHIND INCIDENT AND REFLECTED SHOCKS THROUGH A  $\vec{0}$ .70 Ne - 0.25 H<sub>2</sub> - 0.05 He MIXTURE

		(f) P <sub>1</sub> = 0.05 MM Hg			
INITIAL GAS	(1)				
	P-/P0	6.5789-5	M; NOL WT	14.83221	
	T, DEG K H/RT	298 C.000C	CP/R Ganma .(S)	2.7423 1.5740	
	S/R	27.3693	SON VELIMISEC	512.49	
MACH NO.	29.2460		15.5979 12.6		
U1; M/SEC		12000.00 10000.00	800C.CC 650C	.co 5000.00	
SHEEKEL CAS ()	2358.19	TECEQUILIERIUM 1792.19 1669.45	1534.88 145	6.63 1481.28	
P/P6		6.5643-1 3.9819-1			
T, GEG K	25577	18535 16294		1634 9936 8C45 4.0252	
H/RT S/R	6.8298 21.9081	7.0503 6.3441 23.1410 24.2631		8045 4.0252 9819 27.4895	
M; MOE WT (DLW/CLF)T	6.04504	7.21612 8.21445 -1.11025 -1.09672		1988 11.43644	
(DUV/CLT)P	1.1763	2.3279 2.2137		7719 1.3200	
CP/R	4.5500	23.2744 22.6538		3137 8.5144	
GAMMA (S) Gamma	1.3926 1.4235			1735 1.2258 2406 1.2509	
SON VELIMISEC	699941	4933.5 4328.1		84.8 2975.6	
COLLOMBIC FAR	ANETERS				
IP MER, CM-1	61949	559.5 438.9	307.4 2	C4.0 130.3	
DEBYE LNG, CM		2.0757-6 2.646C-6			
DEBNIBETN	9.1723-11	8.8457-1 9.0132-1	9.2871-1 9.68	25-1 1.0158 0	
NUMBER OF CHA	REEC PARTIO	CLES IN DEBYE SPHE	RE		
	c 5410 C	7.6740 0 8.5645 0	1. 0277 1 1 21	72 1 1 7450 1	
COLE COMPRESS				9905 0.99977	
P5/#2	14.969	12.714 11.262	9,309 8	.362 12.522	
T5/T2	1.673	1.429 1.441		.551 2.972	
M5/M2	C.7651	0.7939 0.8123		8916 0.9560	
RHO\$/RHO2 U5+¥2;N/SEC	6.8694	7.0911 6.3703 12708.64 10634.99		8117 4.0284 8.92 5967.23	
03142487326	10177144	12100004 10054077	0,10,00	0.72 3701.23	
	_			ره - <u>خينيان پي</u> نتان ازليان	
MOLE FRACTION	S				
E	4.9055-1	3.9185-1 3.0772-1	2.0550-1 1.13	43-1 3.6184-2	
H2	6.573-12	1.245 -9 6.121 -9	5.814 -8 2.86	5 -7 1.289 -6	
H2≠ H		6.2962-8 1.3297-7 2.1907-2 4.3408-2			
п Н+		2.2135-1 2.3350-1			
H-	1.0210⊣8	1.2116-7 1.9063-7	3.3984-7 3.66	51-7 2.6760-7	
HE		2.3141-2 2.7435-2 1.1849-3 2.5655-4			
HE+ HE+4		1.207-13 3.663-16			
NE	9.8367-3	1.7124-1 3.1372-1	4.3540-1 4.95	53-1 5.3968-1	
NE+		1.6932-1 7.3958-2			
NE++ NE+++		2.388 -7 4.495 -9 5.251-20 6.378-24			
-···					
PARTICLE DENSITIES, 1/CM++3					
TCTAL		2.614 17 1.801 17	1 107 17 7 52		
16186	J.JJ4 11	COCTA IL TOOR IL	10101 11 1033	C 10 0.230 16	

2.2830-2 2.2693-2 1.5902-2 8.88662-3 3.8154-3 9.1034-4 1.1431-2 1.1362-2 7.9590-3 4.4455-3 1.9082-3 4.5519-4

NEGATIVE EXCESS THERMOCYNAMIC PROPERTIES

- (HIRT) CCLL - (SIR) CCLL



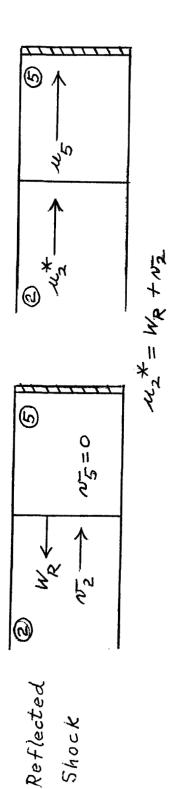


Figure 1. - Comparison between actual and relative velocities

45= NR-105=NR

of gases in a shock tube.

